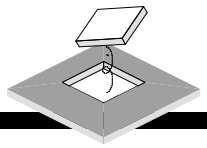

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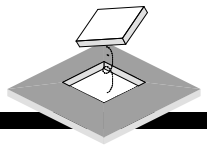

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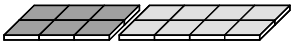

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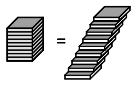
Chapter 7: Equations  **141**

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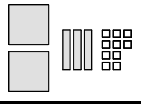
Chapter 9: Polynomials  **221**

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