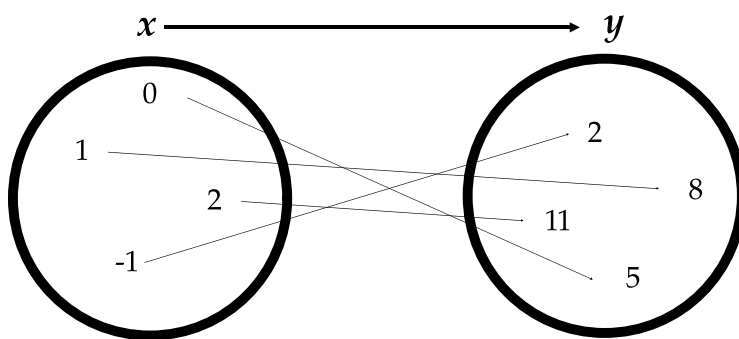

Appendix 4

Functions and Maps

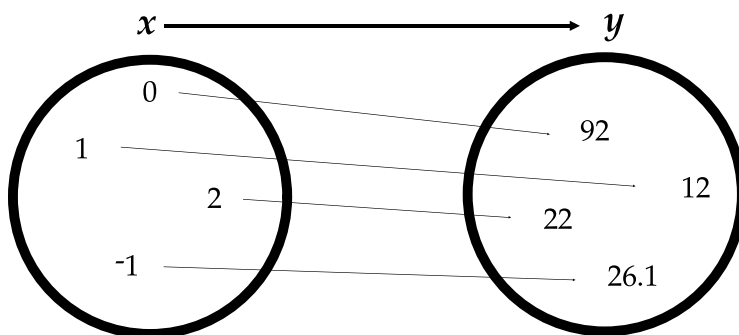
Maps

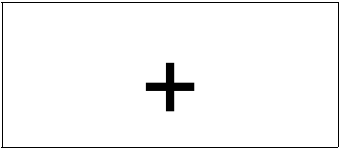
We can illustrate a function with a **map**. A map is a diagram of the x 's and y 's with each x connected to its correct y . The connection is shown by an arrow to remind you that x is first and y is the answer. The rule determines which x goes to which y .



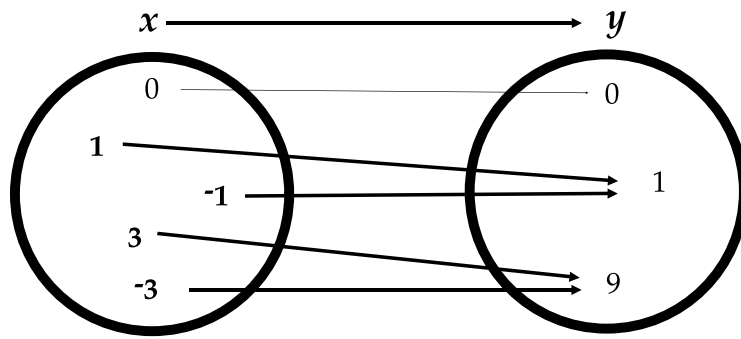
We can draw a map from a list of pairs, even if we do not know the rule:

Pairs are: $(0, 92)$, $(1, 12)$, $(2, 22)$, and $(-1, 26.1)$





Here is a map of the function x^2 :



With some functions, different x 's are mapped to the same y .

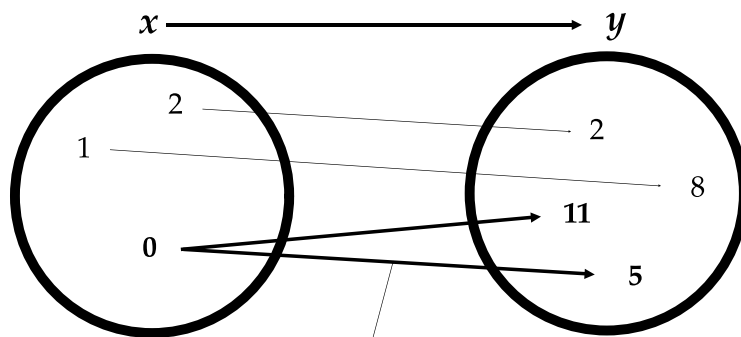
Maps that are Not Functions

Not all maps or lists of pairs are functions. By our previous definition, *the rule had to give the same answer for x each time*. In the game, this means that if 1 is given as x once or several times, the answer will always be the same. *Each x can have only one y as an answer*. We must understand, however, that the chart may have two x 's which share the same y .

The following chart does *not* represent a function because 0 has two *different* answers:

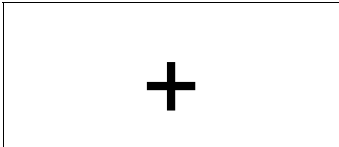
| x | y |
|-----|-----|
| 0 | 5 |
| 1 | 8 |
| 0 | 11 |
| 2 | 2 |

The corresponding map looks like this:



Cannot be a function

Summary



Here is an illustration of what is *not* a function:

- A table, where an x has more than one y :

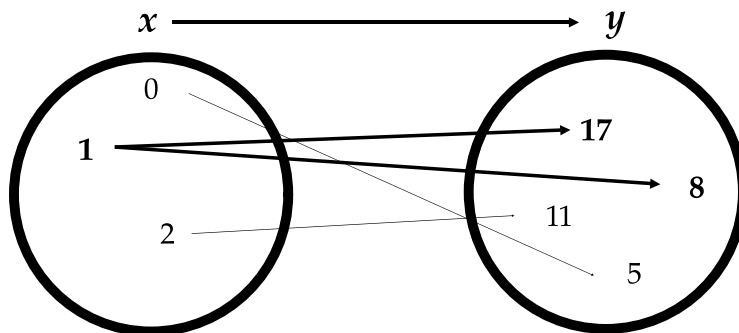
| x | y |
|-----|-----|
| 0 | 5 |
| 1 | 8 |
| 2 | 11 |
| 1 | 17 |

These are *not* functions.

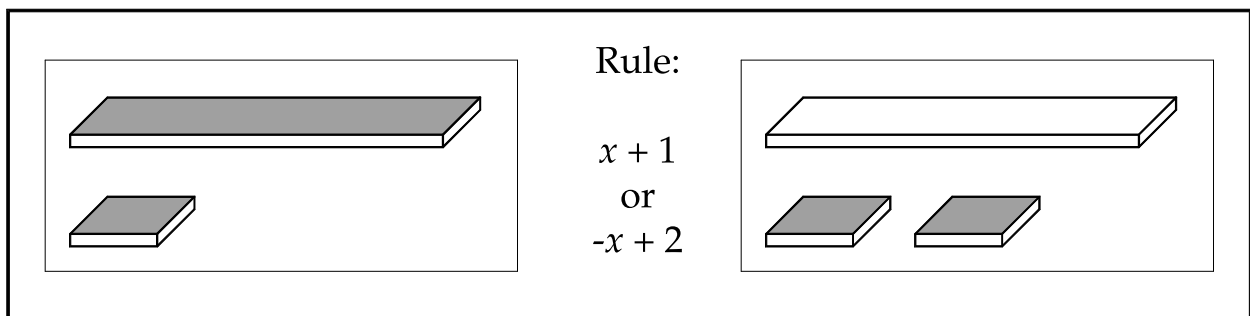
- A list of *ordered pairs*, where an x has more than one y :

$(0, 5), (1, 8), (2, 11), (1, 17)$

- A map, where an x is paired with more than one y :



- A machine, where the rule is not the same every time:



+

Exercises

Finish the tables:

1. $y = 3x^2$

| x | y |
|-----|-----|
| -5 | 75 |
| 5 | ? |
| 10 | ? |
| 3 | ? |
| 1 | ? |
| -1 | ? |

2. $y = x + 2x + 1$

| x | y |
|-----|-----|
| -1 | -2 |
| 0 | 1 |
| 1 | ? |
| 3 | ? |
| 2 | ? |
| -5 | ? |

3. $y = -x + x$

| x | y |
|-----|-----|
| 6 | 0 |
| -4 | ? |
| 0 | ? |
| 2 | ? |
| -3 | ? |
| 17 | ? |

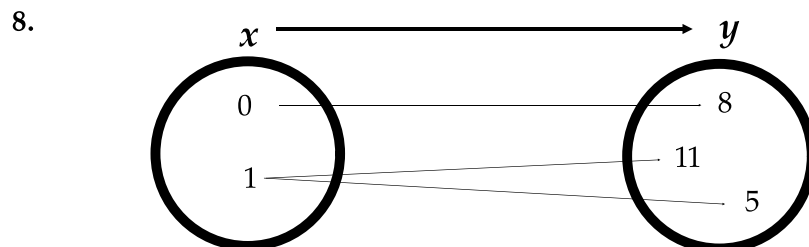
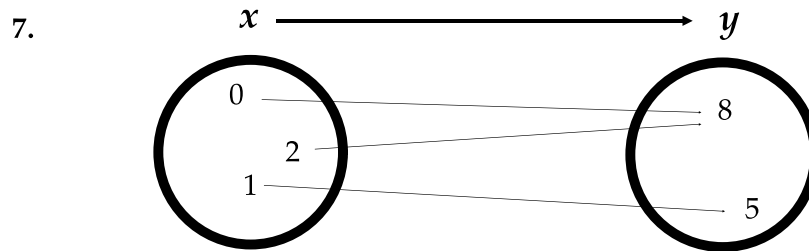
Draw a map for each list of ordered pairs:

4. $(0, 5), (1, 6), (2, 7), (3, 8)$

5. $(0, 5), (3, 5), (-3, 5), (16.3, 5)$

6. $(-3, 11), (6, \sqrt{17}), \left(\frac{3}{2}, 5\right)$

Which of the following maps or charts are functions?



9. $x = 3y^2$

| x | y |
|-----|-----|
| 75 | -5 |
| 75 | 5 |
| 300 | 10 |
| 12 | 2 |
| 0 | 0 |
| -1 | ? |

10.

| x | y |
|-----|------|
| 1 | 17.5 |
| 0 | 17.5 |
| 1 | 17.5 |
| 3 | 17.5 |
| 2 | 17.5 |
| 5 | 17.5 |

11.

| x | y |
|-----|---------------|
| 6 | -6 |
| 6 | 4 |
| 6 | $\frac{3}{2}$ |
| 6 | 6 |
| 1 | 5 |
| -1 | 5 |

